<u>Mathematics</u> <u>Calculation Policy</u>

May 2021

"Mathematical proficiency requires a focus on core knowledge and procedural fluency so that pupils can carry out mathematical procedures flexibly, accurately, consistently, efficiently and appropriately. Procedures and understanding are developed in tandem." NCETM 2014

How we teach mathematics

Mathematics Policy

At Eastfield Infants' and Nursery Academy and Lacey Gardens Junior Academy we recognise that mathematics is essential to everyday life, critical to science, technology and engineering, and necessary for financial literacy and most forms of employment. Therefore, we recognise the importance of a high quality mathematics curriculum. The following policy guides the planning, teaching and assessment of the subject.

This policy should be read in conjunction with other policies and documentation including:

- Curriculum
- Teaching and Learning
- Academic Guidance
- Assessment
- Target Setting
- Intervention
- Equal Opportunities
- School progressions for calculation.
- Linked Learning
- Marking and feedback

Rationale

Through developing a child's ability to calculate, to reason and problem solve, a high quality mathematics education provides a foundation for understanding the world, the ability to reason mathematically, an appreciation of the power of mathematics, and a sense of enjoyment and curiosity about the subject.

Purpose

The aims of Mathematics are:

- to promote enjoyment and enthusiasm for learning through practical activity, exploration and discussion
- for children to become **fluent** in the fundamentals of mathematics so that they are able to recall and apply their knowledge rapidly and accurately
- for children to be able to **reason mathematically** by following a line of enquiry, hypothesising about relationships and generalisations, and developing an argument, justification or proof using mathematical language
- for children to be able to **solve problems** by applying their mathematics to a variety of routine and non-routine problems with increasing sophistication
- for children to be able to demonstrate and develop effective learning behaviours such as: perseverance, collaboration, questioning and organisation
- to develop children's understanding of the importance of Mathematics in everyday life

Our Aims:

- Consistency across school
- Ensure full coverage of the curriculum depth and breadth
- A cyclical approach to teaching maths children can build on previous skills
- Children enjoy doing maths
- Every child CAN succeed 'Positive Mindset'
- Children who can articulate about maths fluent mathematicians!
- Mathematical vocabulary based
- Creative curriculum
- Children are prepared for tests (End of Key Stage tests and Year 4 times table test)
- Sticky learning children don't forget previously taught learning
- Use of CPA across school
- Fluency, thinking, conceptual understanding, procedural understanding and problem solving basically skills for life!

Teaching and Learning

Mathematics is taught as a discrete lesson every day. In KS2, we follow the 'same day intervention approach', whereby teachers deliver the input, the children answer 6/7 diagnostic questions, the questions are marked whilst the children are in assembly and after, the intervention or

deeper thinking tasks will take place. Where possible, all children engage in the objectives specified in the National Curriculum for their year group. Where this is not possible, teachers are expected to differentiate appropriately.

In KS1 each maths lesson looks like...

- 1. Quick maths (for fluency and facts)
- 2. Learning cycle including steps to success
- 3. Independent task mixture of varied fluency, problem solving and reasoning
- 4. Demo and review
- 5. Same Day Intervention / Deeper thinking task- It's not a catch up, it's a keep up!

In KS2 each maths lesson looks like...

- 1. Quick maths (for fluency and facts)
- 2. Learning cycle including steps to success
- 3. Diagnostic task mixture of varied fluency, problem solving and reasoning
- 4. Same Day Intervention / Deeper thinking task- It's not a catch up, it's a keep up!

The fundamentals

- ✓ A belief that every child can and will achieve mastery
- ✓ Bespoke Laceyfield medium term plan
- ✓ A focus on task design everything is done on purpose
- ✓ Blue partner/ Green Partner
- ✓ Quick maths for fluency

- ✓ Knowledge organisers for each unit
- ✓ Same Day Intervention (KS2)
- ✓ All children will reason and problem solve
- ✓ Whole Class Choral Response
- ✓ Learning question and steps to success (created with the class)
- ✓ No ability groupings
- ✓ S planning
- ✓ Conceptual and procedural variation
- ✓ Demo and review phase
- ✓ Up-to-date working walls
- ✓ Concrete Pictorial Abstract
- ✓ Use of resources including pictorial in all year groups
- ✓ A focus on 'grown up mathematical' vocabulary
- ✓ Pace, productivity, progress
- Bar modelling Children use Times Tables Rockstars

Planning

- Teachers use the Laceyfield Bespoke medium term plans alongside the Ready to Progress Criteria. This highlights when each strand should be taught throughout the year. This plan provides adequate time to be spent on each unit in order for children to achieve depth.
- We also believe in a cyclical approach to teaching maths as we strongly believe children learn best when small steps are continuously revisited, built on and deepened. Therefore, most units are revisited in the summer term.
- The Ready To Progress document is used to inform planning and ensure the curriculum is prioritised
- Teachers use Whiterose to break each objective down into small steps.
- A large range of resources are used from various websites including NCETM, I See Reasoning, Whiterose, Classroom Secrets and Master the Curriculum in order to design tasks to suit the children's needs.
- Short term planning will be flexible and responsive to the children's needs that are identified through every day formative assessment this is usually done in the form of a 'S-Plan.'
- When introducing a new concept to children in all year groups it is important that teachers use the following planning cycle: 1) Practical exploration of the concept with resources. 2) Visual representations used to aid the transition from practical to written activities. 3) Abstract application. 4) Opportunities to reason with and apply the new skills learnt in an unfamiliar or challenging context.

• Although mental maths tests have been removed from the Year 6 assessments, mental capabilities are still vital for expected arithmetic standards set out within the National Curriculum. This should be reflected in mental maths teaching within lessons (quick maths).

Teaching

- 1. With an increased emphasis on written calculation within the National Curriculum, it is important that teachers consistently follow agreed progressions for the teaching of calculation and that the method for written calculation is developed alongside the use of practical resources (e.g. straws and counters) to ensure a secure conceptual understanding.
- 2. Resources to support children should be available in every classroom and the children should be taught how to self-select equipment that could support their learning.
- 3. Teachers should adopt a flexible grouping policy which either utilises mixed ability partners or partners who have been matched to the specific lesson and previous assessment. (See Teaching and Learning policy for more information.)
- 4. Teaching Assistants should contribute to the children's learning within the lesson in the way identified on the teacher's planning.
- 5. Staff will all have high expectations of all children and ensure that they are challenged at an appropriate level and that they can achieve their full potential.
- 6. Each classroom should have a maths 'working wall' which will be updated regularly. Items on the wall should help to support children with independent learning and could include: Reminders about key vocabulary, a WAGOLL of how to solve a particular problem, steps to success, examples of children's successful work, celebration of mistakes or evidence of the learning journey completed throughout a lesson or maths unit.

Key Vocabulary

It is important that teachers model correct mathematical language and use this at all times.

The four mathematical operations should be referred to as 'addition', 'subtraction', 'multiplication' and 'division'. There are two models of subtraction, take-away and difference, and two models of division, sharing and grouping. It is important that children understand the distinction between these models.

'Borrowing' is an incorrect term to use when referring to the exchanging of digits when completing column subtraction as it implies that the digit will be given back. The process is known as 'exchange' and the correct terminology must be used.

'Carrying' of digits is correct terminology when referring to formal written methods and must be used.

The Key Stage 1 and 2 Programmes of Study for Maths details the formal written methods of columnar addition and subtraction, long and short multiplication and long and short division in appendix 1.

<u>https://www.gov.uk/government/uploads/system/uploads/attachment_data/file/335158/PRIMARY_national_curriculum_-_Mathematics_220</u> 714.pdf

Assessment

Maths is assessed regularly through various means.

Teachers gather ongoing evidence during lessons, through the use of assessment for learning techniques, observations and marking and feedback which contributes to their assessment of children against the criteria set out in the National Curriculum which demonstrates the age-related expectations for each year group. In KS2, we also assess children every term using Whiterose Maths end of unit formal assessments. They formalise these assessments at key assessment points by completing a point in time assessment criteria sheet for each child, supported by the delivery of progress tests in Maths and teacher assessments. In KS1, cold tasks are used to support teacher assessments alongside fluency based quick maths activities. The amount of criteria the child is successfully demonstrating, with secure application, translates into an overall judgement which gives a view of how well the child is progressing towards meeting age-related expectations and / or their individual targets (see assessment policy for more detailed information).

Cross Curricular Learning

We are strong believers that the Eastfield Infants' and Nursery Academy and Lacey Gardens Junior Academy Curriculum should equip children for real life. We therefore aim to integrate measure and statistics into our 'Project based learning' where possible. This ensures that the maximum amount of time is spent rehearsing, using and applying the skills learned in core subjects in order that these are secure and well embedded for children who in turn grow to appreciate the transference and, crucially, the importance of these skills.

Monitoring and Review

The mathematics leaders have a responsibility for monitoring the standard of the children's work and the quality of the teaching in mathematics. The mathematics leaders are also responsible for supporting colleagues in the teaching of Mathematics, for being informed about current developments in the subject and for providing a strategic lead and direction for the subject in the school. The mathematics leaders will keep an up to date record of the subject policy, causal chains, an action plan for improving the subject, relevant and analysed school data, evidence of subject monitoring and any other information relevant to the subject or role. Once per term we allocate special time for the vital task of monitoring and evaluation as part of school self-evaluation procedures.

Progression in Mental Calculation

These objectives have been adapted from 'Teaching Children to Calculate Mentally' (2010), which was based on the old primary frameworks so additional elements from the 2014 curriculum have been included.

Addition and Subtraction

Recall:	Mental calculation skills:	Mental methods or strategies:
Children should be able to	Working mentally, with jottings if needed, children should be able to:	Children should understand when to
derive and recall:		and be able to apply these strategies:
Year 1 • number pairs with a total of 10, e.g. $3 + 7$, or what to add to a single-digit number to make 10, e.g. $3 + \Box = 10$ • addition facts for totals to at least 5, e.g. $2 + 3$, $4 + 3$ • addition doubles for all numbers to at least 10, e.g. 8 + 8	 add or subtract a pair of single-digit numbers, e.g. 4 + 5, 8 - 3 add or subtract a single-digit number to or from a teens number, e.g. 13 + 5, 17 - 3 add or subtract a single-digit to or from 10, and add a multiple of 10 to a single-digit number, e.g. 10 + 7, 7 + 30 	 reorder numbers when adding, e.g. put the larger number first count on or back in ones, twos or tens partition small numbers, e.g. 8 + 3 = 8 + 2 + 1 partition and combine tens and ones

Recall: Children should be able to derive and recall:	Mental calculation skills: Working mentally, with jottings if needed, children should be able to:	Mental methods or strategies: Children should understand when to and be able to apply these strategies:
Year 2 • addition and subtraction facts for all numbers up to at least 10, e.g. $3 + 4$, $8 - 5$ • addition and subtraction facts for all numbers to 20 fluently, e.g. $13 + 4$, $18 - 7$ • number pairs with totals to 20 • all pairs of multiples of 10 with totals up to 100, e.g. 30 + 70, or 60 + \Box = 100 • what must be added to any two-digit number to make the next multiple of 10, e.g. $52 + \Box$ = 60 • addition doubles for all numbers to 20, e.g. 17 + 17 and multiples of 10 to 50, e.g. 40 + 40	 add or subtract a pair of single-digit numbers, including crossing 10, e.g. 5 + 8, 12 - 7 add any single-digit number to or from a multiple of 10, e.g. 60 + 5 subtract any single-digit number from a multiple of 10, e.g. 80 - 7 add or subtract a single-digit number to or from a two-digit number, including crossing the tens boundary, e.g. 23 + 5, 57 - 3, then 28 + 5, 52 - 7 add or subtract a multiple of 10 to or from any two-digit number, e.g. 27 + 60, 72 - 50 add 9, 19, 29, or 11, 21, 31, subtract mentally a two-digit number from another two-digit number when there is no regrouping required (e.g. 74 - 33) add three single digit numbers eg 6 + 1 + 4 	 reorder numbers when adding partition: bridge through 10 and multiples of 10 when adding and subtracting partition and combine multiples of tens and ones use knowledge of pairs making 10 partition: count on in tens and ones to find the total partition: count on or back in tens and ones to find the difference partition: add a multiple of 10 and adjust by 1
Year 3 • addition and subtraction facts for all numbers to 20, e.g. 9 + 8, 17 – 9, drawing on knowledge of inverse operations	 add and subtract groups of small numbers, e.g. 5 – 3 + 2 add or subtract a two-digit number to or from a multiple of 10, e.g. 50 + 38, 90 – 27 add or subtract any pair of two-digit numbers, including crossing the tens and 100 boundary, e.g. 47 + 58, 91 – 35 (from Y4) add and subtract numbers mentally, including: oa three-digit number and ones oa three-digit number and tens 	 count on or back in hundreds, tens, ones, tenths reorder numbers when adding identify pairs totalling 10 or multiples of 10 partition: add tens and ones separately, then recombine

• sums and differences of multiples of 10, e.g. 50 + 80,	oa three-digit number and hundreds	 partition: count on in tens and ones to find the total
120 – 90		partition: count on or back in tens and
• pairs of two-digit numbers		ones to find the difference
with a total of 100, e.g. 32 +		 partition: add or subtract 10 or 20 and
68, or 32 + □ = 100		adjust
 addition doubles for 		 partition: count on or back in minutes
multiples of 10 to 100, e.g.		and hours, bridging through 60 (analogue
90 + 90		times)

Recall: Children should be able to derive and recall:	Mental calculation skills: Working mentally, with jottings if needed, children should be able to:	Mental methods or strategies: Children should understand when to and be able to apply these strategies:
 Year 4 sums and differences of pairs of multiples of 10, 100 or 1000 addition doubles of numbers 1 to 100, e.g. 38 + 38, and the corresponding halves what must be added to any three-digit number to make the next multiple of 100, e.g. 521 + □ = 600 pairs of fractions that total 1 	 add or subtract a near multiple of 10, e.g. 56 + 29, 86 - 38 find a small difference by counting up, e.g. 72 - 68, 211 - 196 add or subtract two-digit or three-digit multiples of 10, e.g. 120 - 40, 140 + 150, 370 - 180 add or subtract a near multiple of 10 or 100 to any two-digit or three-digit number, e.g. 235 + 198 (from Y5) add or subtract a pair of two-digit numbers or three-digit multiples of 10, e.g. 38 + 86, 620 - 380, 350 + 360 (from Y5) 	 count on or back in hundreds, tens, ones, tenths and hundredths partition: add tens and ones separately, then recombine partition: subtract tens and then ones, e.g. subtracting 27 by subtracting 20 then 7 subtract by counting up from the smaller to the larger number partition: add or subtract a multiple of 10 and adjust, e.g. 56 + 29 = 56 + 30 - 1, or 86 - 38 = 86 - 40 + 2 partition: double and adjust use knowledge of place value and related calculations, e.g. work out 140 + 150 = 290 using 14 + 15 = 29 partition: count on or back in minutes and hours, bridging through 60 (analogue and digital times)

 • sums and differences of decimals, e.g. 6.5 + 2.7, 7.8 - 1.3 • doubles and halves of decimals, e.g. half of 5.6, double 3.4 • what must be added to any four-digit number to make the next multiple of 1000, e.g. 4087 + □ = 5000 • what must be added to a decimal with units and tenths to make the next whole number, e.g. 7.2 + □= • Ind the difference of 1000, e.g. 6070 - 4 • add or subtract a tenths, e.g. 5.7 + 2 • add or subtract a four-digit number, • add or subtract a number, not crossi 	e between near multiples of 100, e.g. 607 – 588, or of 087 ny pairs of decimal fractions each with units and 5, 6.3 – 4.8 near multiple of 10 or 100 to any three-digit or e.g. 235 + 198 multiple of 10, 100 or 1000 to a four or five-digit ng boundary, e.g. 12,462 - 2300	 count on or back in hundreds, tens, ones and tenths partition: add hundreds, tens or ones separately, then recombine subtract by counting up from the smaller to the larger number add or subtract a multiple of 10 or 100 and adjust partition: double and adjust use knowledge of place value and related calculations, e.g. 6.3 – 4.8 using 63 – 48 partition: count on or back in minutes and hours, bridging through 60 (analogue and digital times)
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Recall: Children should be able to derive and recall:	Mental calculation skills: Working mentally, with jottings if needed, children should be able to:	Mental methods or strategies: Children should understand when to and be able to apply these strategies:
Year 6	• add or subtract pairs of decimals with units, tenths or hundredths, e.g.	 count on or back in hundreds, tens,
 addition and subtraction 	0.7 + 3.38	ones, tenths and hundredths
facts for multiples of 10 to	 find doubles of decimals each with units and tenths, e.g. 1.6 + 1.6 	 use knowledge of place value and
1000 and decimal numbers	 add near doubles of decimals, e.g. 2.5 + 2.6 	related calculations, e.g. 680 + 430, 6.8 +
with one decimal place, e.g.	• add or subtract a decimal with units and tenths, that is nearly a whole	4.3, 0.68 + 0.43 can all be worked out
650 + □ = 930, □− 1.4 = 2.5	number, e.g. 4.3 + 2.9, 6.5 – 3.8	using the related calculation 68 + 43
 what must be added to a 	•Calculate mentally, using efficient strategies such as manipulating	 use knowledge of place value and of
decimal with units, tenths	expressions using commutative and distributive properties to simplify	doubles of two-digit whole numbers
and hundredths to make the	the calculation	 partition: double and adjust
next whole number, e.g.	(e.g. 53 – 82 + 47 = 53 + 47 – 82 = 100 – 82 = 18)	 partition: add or subtract a whole
7.26 + □= 8	•Use their knowledge of the order of operations to carry out calculations	number and adjust, e.g. 4.3 + 2.9 = 4.3 + 3
	involving the 4 operations, e.g. $4 \times 2 + 3 \times 5$	-0.1, 6.5 - 3.8 = 6.5 - 4 + 0.2

	• partition: count on or back in minutes
	and hours, bridging through 60 (analogue
	and digital times, 12-hour and 24-hour
	clock)

Multiplication and Division

Recall: Children should be able to derive and recall:	Mental calculation skills: Working mentally, with jottings if needed, children should be able to:	Mental methods or strategies: Children should understand when to and be able to apply these strategies:
Year 1 • doubles of all numbers to 10, e.g. double 6 • odd and even numbers to 20	• count on from and back to zero in ones, twos, fives or tens	• use patterns of last digits, e.g. 0 and 5 when counting in fives
Year 2 • doubles of all numbers to 20, e.g. double 13, and corresponding halves • doubles of multiples of 10 to 50, e.g. double 40, and corresponding halves • multiplication facts for the 2, 5 and 10 times-tables, and corresponding division facts • odd and even numbers to 100	 double any multiple of 5 up to 50, e.g. double 35 halve any multiple of 10 up to 100, e.g. halve 90 find half of even numbers to 40 find the total number of objects when they are organised into groups of 2, 5 or 10 	 partition: double the tens and ones separately, then recombine use knowledge that halving is the inverse of doubling and that doubling is equivalent to multiplying by two use knowledge of multiplication facts from the 2, 5 and 10 times-tables, e.g. recognise that there are 15 objects altogether because there are three groups of five
Year 3 • multiplication facts for the 2, 3, 4, 5, 8 and 10 times-tables, and corresponding division facts • doubles of multiples of 10 to 100, e.g. double 90, and corresponding halves	 double any multiple of 5 up to 100, e.g. double 35 halve any multiple of 10 up to 200, e.g. halve 170 multiply one-digit or two-digit numbers by 10 or 100, e.g. 7 × 100, 46 × 10, 54 x 100 find unit fractions of numbers and quantities involving halves, thirds, quarters, fifths and tenths double any two-digit number, e.g. double 39 (from Y4) multiply a multiple of 10 to 100 by a single-digit number (linked to the tables they know), e.g. 40 × 3 (from Y4) 	 partition: when doubling, double the tens and ones separately, then recombine partition: when halving, halve the tens and ones separately, then recombine use knowledge that halving and doubling are inverse operations recognise that finding a unit fraction is equivalent to dividing by the denominator and use knowledge of division facts

 multiplication and division facts (for example, using 3 × 2 = 6, 6 - 2 and 2 = 6 ÷ 3) to derive related facts (for example, 30 × 2 = 60, 6 3 = 20 and 20 = 60 ÷ 3). 	 3 = • recognise that when multiplying by 10 or 100 the digits move one or two places to the left and zero is used as a place holder • Using doubling, they connect the 2, 4 and 8 multiplication tables. • use knowledge of multiplication facts and place value, e.g. 7 x 8 = 56 to find 70 x 8, 7 x 80 (from Y4)
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Recall:	Mental calculation skills:	Mental methods or strategies:
Children should be able to	Working mentally, with jottings if needed, children should be able	Children should understand when to and be
derive and recall:	to:	able to apply these strategies:
Year 4 • multiplication facts to 12 × 12 and the corresponding division facts • doubles of numbers 1 to 100, e.g. double 58, and corresponding halves • doubles of multiples of 10 and 100 and corresponding halves • fraction and decimal equivalents of one-half, quarters, tenths and hundredths, e.g. 3/10 is 0.3 and 3/100 is 0.03 • factor pairs for known multiplication facts	 double any multiple of 10 or 100, e.g. double 340, double 800, and halve the corresponding multiples of 10 and 100 halve any even number to 200 find unit fractions and simple non-unit fractions of numbers and quantities, e.g. 3/8 of 24 multiply and divide numbers to 1000 by 10 and then 100 (whole-number answers), e.g. 325 × 10, 42 × 100, 120 ÷ 10, 600 ÷ 100, 850 ÷ 10 multiply numbers to 20 by a single-digit, e.g. 17 × 3 identify the remainder when dividing by 2, 5 or 10 give the factor pair associated with a multiplication fact, e.g. identify that if 2 x 3 = 6 then 6 has the factor pair 2 and 3 multiply together three numbers 	 use understanding that when a number is multiplied or divided by 10 or 100, its digits move one or two places to the left or the right and zero is used as a place holder use partitioning and the distributive law to multiply, e.g.13 × 4 = (10 + 3) × 4 = (10 × 4) + (3 × 4) = 40 + 12 = 52 combine their knowledge of number facts and rules of arithmetic to solve mental and written calculations for example, 2 x 6 x 5 = 10 x 6 = 60. Pupils practise mental methods and extend this to three-digit numbers to derive facts, (for example 600 ÷ 3 = 200 can be derived from 2 x 3 = 6).

	Recall:	Mental calculation skills:	Mental methods or strategies:
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Children should be able to	Working mentally, with jottings if needed, children should be able	Children should understand when to and be able
derive and recall:	to:	to apply these strategies:
Year 5	• multiply and divide two-digit numbers by 4 or 8, e.g. 26 × 4, 96 ÷ 8	 multiply or divide by 4 or 8 by repeated
 squares to 12 × 12 	• multiply two-digit numbers by 5 or 20, e.g. 320 × 5, 14 × 20	doubling or halving
 division facts 	• multiply by 25 or 50, e.g. 48 × 25, 32 × 50	• form an equivalent calculation, e.g. to multiply
corresponding to tables up	• double three-digit multiples of 10 to 500, e.g. 380 × 2, and find the	by 5, multiply by 10, then halve; to multiply by 20,
to 12 × 12, and the related	corresponding halves, e.g. 760 ÷ 2	double, then multiply by 10
unit fractions, e.g. 7 × 9 = 63	 find the remainder after dividing a two-digit number by a 	 use knowledge of doubles/halves and
so one-ninth of 63 is 7 and	single-digit number, e.g. 27 ÷ 4 = 6 R 3	understanding of place value, e.g. when
one-seventh of 63 is 9	 multiply and divide whole numbers and decimals by 10, 100 or 	multiplying by 50 multiply by 100 and divide by 2
 decimal and percentage 	1000, e.g. 4.3 × 10, 0.75 × 100, 25 ÷ 10, 673 ÷ 100, 74 ÷ 100	 use knowledge of division facts, e.g. when
equivalents of one-half,	• multiply pairs of multiples of 10, e.g. 60 × 30, and a multiple of 100	carrying out a division to find a remainder
one-quarter, three-quarters,	by a single digit number, e.g. 900 × 8	 use understanding that when a number is
tenths and hundredths	 divide a multiple of 10 by a single-digit number (whole number 	multiplied or divided by 10 or 100, its digits move
 factor pairs to 100 	answers) e.g. 80 ÷ 4, 270 ÷ 3	one or two places to the left or the right relative
• p rime numbers up to 20.	• find fractions of whole numbers or quantities, e.g. 23 of 27, 45 of 70	to the decimal point, and zero is used as a place
	kg	holder
	• find 50%, 25% or 10% of whole numbers or quantities, e.g. 25% of	 use knowledge of multiplication and division
	20 kg, 10% of £80	facts and understanding of place value, e.g. when
	• find factor pairs for numbers to 100, e.g. 30 has the factor pairs 1 ×	calculating with multiples of 10
	30, 2 × 15, 3 × 10 and 5 × 6	 use knowledge of equivalence between
		fractions and percentages, e.g. to find 50%, 25%
		and 10%
		 use knowledge of multiplication and division
		facts to find factor pairs

Recall:	Mental calculation skills:	Mental methods or strategies:
Children should be able to	Working mentally, with jottings if needed, children should be able	Children should understand when to and be able
derive and recall:	to:	to apply these strategies:
Year 6 • squares to 12 × 12	 multiply pairs of two-digit and single-digit numbers, e.g. 28 × 3 divide a two-digit number by a single-digit number, e.g. 68 ÷ 4 divide by 25 or 50, e.g. 480 ÷ 25, 3200 ÷ 50 	• partition: use partitioning and the distributive law to divide tens and ones separately, e.g. $92 \div 4$ = (80 + 12) $\div 4 = 20 + 3 = 23$

 squares of the 	• double decimals with units and tenths, e.g. double 7.6, and find the	• form an equivalent calculation, e.g. to divide by
corresponding multiples of	corresponding halves, e.g. half of 15.2	25, divide by 100, then multiply by 4; to divide by
10	• multiply pairs of multiples of 10 and 100, e.g. 50 × 30, 600 × 20	50, divide by 100, then double
• equivalent fractions,	• divide multiples of 100 by a multiple of 10 or 100 (whole number	 use knowledge of the equivalence between
decimals and percentages	answers), e.g. 600 ÷ 20, 800 ÷ 400, 2100 ÷ 300	fractions and percentages and the relationship
for hundredths, e.g. 35% is	• multiply and divide two-digit decimals such as 0.8 × 7, 4.8 ÷ 6	between fractions and division
equivalent to 0.35 or 35/100	• find 10% or multiples of 10%, of whole numbers and quantities, e.g.	 recognise how to scale up or down using
	30% of 50 ml, 40% of £30, 70% of 200 g	multiplication and division, e.g. if three oranges
	 simplify fractions by cancelling 	cost 24p:one orange costs 24 ÷ 3 = 8p four
	• identify numbers with odd and even numbers of factors and no	oranges cost 8 × 4 = 32p
	factor pairs other than 1 and themselves	• Use knowledge of multiplication and division
		facts to identify factor pairs and numbers with
		only two factors

Progression in written calculations

Each strategy is first taught through concrete representations before moving on to pictorial and then abstract representations. This will ensure that pupils develop depth of understanding. However, if a pupil is struggling with an abstract or pictorial representation when they move onto a new stage of calculation (e.g. progressing from using column subtraction for whole numbers to decimals), they should be moved back to an abstract or pictorial representation to support their understanding before returning to the abstract. Concrete and pictorial representations should be used in all age groups.

	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Addition	Combining two parts to make a whole: part whole model. Starting at the bigger number and counting on. Regrouping to make 10.	Adding three single digits. Column method – grouping and regrouping. Use concrete and pictorial representations with base 10. No abstract representations in Y2.	Column method- regrouping. (up to 3 digits)	Column method- regrouping. (up to 4 digits)	Column method- regrouping. (with more than 4 digits) (Decimals- with the same amount of decimal places)	Column method- regrouping. (Decimals- with different amounts of decimal places)
Subtraction	Taking away ones Counting back Find the difference Part whole model Make 10	Counting back Find the difference Part whole model Make 10 Column method – grouping and regrouping. Use concrete and pictorial representations with base 10. No abstract representations in Y2.	Column method with regrouping. (up to 3 digits)	Column method with regrouping. (up to 4 digits)	Column method with regrouping. (with more than 4 digits) (Decimals- with the same amount of decimal places)	Column method with regrouping. (Decimals- with different amounts of decimal places)
Multiplicatio n	Doubling Counting in multiples Arrays (with support)	Doubling Counting in multiples Repeated addition	Counting in multiples Repeated addition Arrays- showing commutative multiplication	Column multiplication (2 and 3 digit multiplied by 1 digit)	Column multiplication (up to 4 digit numbers multiplied by 1 or 2 digits)	Column multiplication (multi digit up to 4 digits by a 2 digit number, this includes a decimal

Calculation strategies – matched to year group expectations.

		Arrays- showing commutative multiplication	Grid method			number multiplied by a whole number).
Division	Sharing objects into groups Division as grouping	Division as grouping Division within arrays	Division within arrays Division with a remainder Short division (2 digits by 1 digit- concrete and pictorial)	Division within arrays Division with a remainder Short division (up to 3 digits by 1 digit)	Short division (up to 4 digits by a 1 digit number interpret remainders appropriately for the context)	Short division Long division (up to 4 digits by a 2 digit number- interpret remainders as whole numbers, fractions or round)

Progression in Calculations

Addition

Objective and	Concrete	Pictorial	Abstract
Strategies			

ning two parts to make a whole: part- whole 4 + 3 = 7Þ Þ part model 5 whole 10= 6 + 4 part Starting at the bigger number and counting 12 + 5 = 175 + 12 = 17on Start with the larger number on the bead string and then count on to the 10 11 12 13 14 15 16 17 18 19 20 smaller number 1 by 1 to find the Place the larger number in answer. Start at the larger number on the number line and count your head and count on the on in ones or in one jump to find the answer. smaller number to find your answer Regrouping to make 7 + 4= 11 10. group or partition the If I am at seven, how many more do I need to make 10.

	6 + 5 = 11 Start with the bigger number and use the smaller number to make 10.		How many more do I add on now?
Adding three single digits	4 + 7 + 6= 17 Put 4 and 6 together to make 10. Add on 7. Image:		4 + 7 + 6 = 10 + 7 $= 17$ Combine the two numbers that make 10 and then add on the remainder.
Column method- no regrouping	24 + 15= Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters. T O T O O O O O O O O O O O O O O	After practically using the base 10 blocks and place value counters, children can draw the counters or base 10 to help them to solve additions.	$\frac{Calculations}{21 + 42 =}$ $\frac{21}{42}$

Column method-	Begin v	with Base	10 to help	children	Children can draw a pictoral representation of the	
regrouping	Clearly	see that 1	LU ones ec O Then m	ove on to	columns and base 10/place value counters to further	Start by partitioning the
	place v	alue coun	ters in KS2	2.		to clearly show the
					Pictorial representation of base 10	exchange below the
	Make t	oth numl	pers on a p	olace value	54 + 27 =	addition.
	grid.				te Torder en des teur Mense Marie Nan de Constructionale. La construction de	20 + 5
					Description Company E.F. (as a C + 2 + 2 + 2 + 2 + 2 + 2 + 2 + 2 + 2 +	40 + 8
	(initial content)			146	T O	60 + 13 = 73
	(iii)	0000		<u>+ 527</u>		
	 					536
	$ \check{\odot}\check{\odot}\check{\odot}$				8 +1	As the children ± 85
	Add up	the units	and excha	ange 10 ones		move on, <u>621</u>
	for one	e 10.			ierri las 3 lapinonya til 1 1 and 1	introduce 11
						decimals with the same number of
					Pictorial representation of place value counters	

Abbre readed 0⁻⁻ - SAP Science Str. Hor. Soc. Texp. + + 0⁻ 2634 + 4517 = decimal Calculations 72.8 places and 10 146 (*** +54.6<u>+ 527</u> 127.4 ... 11 3 1 . 1 4 0 • • . . 0 0 7 3 5 different. Money can be . . 2 3 . 3 6 1 Add up the rest of the columns, 7 1 5 9 0 8 0 1 . exchanging the 10 counters from one 59.7 7 0 column for the next place value column + 1 . 3 0 0 • ٠ until every column has been added. 5 9 3 1 2 1 2 As children move on to decimals, used here. money and decimal place value counters can be used to support learning.

Eastfield Infants' and Nursery Academy and Lacey Gardens Junior Academy

Subtraction

Objective and	Concrete	Pictorial	Abstract
Strategies			

away ones	Use physical objects, counters, subes	Cross out drawn objects to show what has been taken	18 -3= 15
	etc to show how objects can be taken	away.	8 – 2 = 6
	away. 6-2=4	$ \begin{array}{c} & & & & & & \\ & & & & & & \\ & & & & & $	
Counting back	Make the larger number in your subtraction. Move the beads along your	Count back on a number line or number track	Put 13 in your head, count back 4. What number are
	bead string as you count backwards in ones.	9 10 11 12 13 14 15	you at? Use your fingers to help.
	13 – 4	Start at the bigger number and count back the smaller number showing the jumps on the number line.	
	Use counters and move them away from the group as you take them away counting backwards as you go.	$\begin{array}{c} -1 & -10 \\ -1 & -1 & -1 \\ 34 & 35 & 36 & 37 \end{array}$	
		This can progress all the way to counting back using two 2 digit numbers.	



	Make 14 on the ten frame. Take away the four first to make 10 and then takeaway one more so you have taken away 5. You are left with the answer of 9.	13 - 7 = 6 3 4 5 1 2 3 4 5 0 7 8 9 10 11 12 13 14 15 16 17 18 19 20 Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.	How many do we have left to take off?
Column method without regrouping	$\int_{1}^{Ters} \int_{1}^{Ones} \int_{$	Draw the Base 10 or place value counters alongside the written calculation to help to show working. $43 - 21 = 22$ $\boxed{\boxed{12}}$	$47 - 24 = 23$ $-\frac{40 + 7}{20 + 3}$ This will lead to a clear written column subtraction. 32 -12 20
Column method with regrouping	Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges.	Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make.	$836 - 254 = 582$ $\frac{360}{130} + \frac{3}{130} + \frac{3}{130$



Now I can take away eight tens and complete my subtraction	
Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount	

Multiplication

Objective and Strategies	Concrete	Pictorial	Abstract
ng	Use practical activities to show how to double a number.	Draw pictures to show how to double a number. Double 4 is 8	$\begin{array}{c} 16\\ 10\\ 12\\ 20\\ 20\\ 12\\ \end{array}$

ng in multiples	Count in multiples supported by concrete objects in equal groups.	$\frac{3}{6} + \frac{3}{6} + \frac{3}$	Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25, 30
ted addition		There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there? 2 add 2 add 2 equals 6 5 + 5 + 5 = 15 5 + 5 + 5 = 15	Write addition sentences to describe objects and pictures.

- showing commutati multiplicati	ve Create arrays using counters/ cubes to show multiplication sentences.	Draw arrays in different rotations to find commutative multiplication sentences.	Use an array to write multiplication sentences and reinforce repeated addition.
		Link arrays to area of rectangles.	5 + 5 + 5 = 15 3 + 3 + 3 + 3 + 3 = 15 5 x 3 = 15 3 x 5 = 15
lethod	Show the link with arrays to first introduce the grid method.	Children can represent the work they have done with place value counters in a way that they understand. They can draw the counters, using colours to show different amounts or just use circles in the different	Start with multiplying by one digit numbers and showing the clear addition alongside the grid.
		columns to show their thinking as shown below.	X 30 5
	Move on to using Base 10 to move towards a more compact method.	$24 \times 3 = 72$	7 210 35 210 + 35 = 245 35
	4 rows of 13	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Moving forward, multiply by a 2 digit number showing the different rows within the grid method.



		1	1
n multiplication	Make links to grid method	Bar modelling and number lines can support	Start with short multiplication,
		learners when solving problems with	reminding the children about lining
	Children can continue to be supported	multiplication alongside the formal written	up their numbers clearly in columns.
	by place value counters at the stage of	methods.	
	multiplication.		If it helps, children can write out what
			they are solving next to their answer
	4	59 59 59 59 59 59 59 59 59 59	
		1 <u>1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 </u>	This moves to the more compact
	3	8 × 59	mathed
		$= 8 \times 60 - 8$ $8 \times 6 = 48$	metriou.
		e + (D = 480	
		480 - 8 = (472)	
	64×3=192		
		10 Litres or 10000 mL	
		# 4 260 . 8 4 250 J 16 4 250 J	The state where there are an and the state are state and the state of
		4 + 250ml 4+250ml a stand	
	It is important at this stage that they	1L IL 41 6L 10L	
	always multiply the ones first and note	4 + 4 + 8 + 8 + 16	
	down their answer followed by the tens	5 x 8 = 40 jugs-	32 1 2
	which they note below.		x 24 1 2 4
			8 (4 x 2) <u>× 2 6</u>
			120 (4 x 30) 7 4 4
			40 (20 x 2) 2 4 8 0
			600 (20 x 30) 3 2 2 4
			768
			6.1 x 15 =

$ \begin{array}{c} 5 \\ + 1 \\ - 1 \\ + 1 \\ - 1 \\ + 1 \\ + 5 \\ - 1 \\ $		
$ \frac{1 + 5}{3 + 3 + 5} \\ \frac{3 + 4}{1 + 4} \\ \frac{1 + 5}{1 + 4} $		
		x 1 3 3 0 3 4 1 0 4 1 0 3

Division

Objective and	Concrete	Pictorial	Abstract
Strategies			

g objects into groups	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities.	Share 9 buns between three people. 9 ÷ 3 = 3
n as grouping	Use cubes, counters, objects or place value counters to aid understanding. I have 10 cubes. How many lots of 2 can you make? How many 5s are there in 35? 0 5 10 15 20 25 30 35	Use a number line to show jumps in groups. The number of jumps equals the number of groups. 0 1 2 3 4 5 6 7 8 9 10 11 12 	28 ÷ 7 = 4 How many 7s are there in 28?

n within arrays	Link division to multiplication by creating an array and thinking about the number sentences that can be created. Eg $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$	Image: Constraint of the series of the se	Find the inverse of multiplication and division sentences by creating four linking number sentences. 7 x 4 = 28 4 x 7 = 28 28 ÷ 7 = 4 28 ÷ 4 = 7
n with a remainder	14 ÷ 3 = Divide objects between groups and see how much is left over	Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder. 0 4 8 12 13 Draw dots and group them to divide an amount and clearly show a remainder.	Complete written divisions and show the remainder using r. $29 \div 8 = 3 \text{ REMAINDER 5}$ $\uparrow \uparrow \uparrow \uparrow$ dividend divisor guotient remainder



	We look how much in 1 group so the answer is 14.		
ivision	Instant Instant <t< td=""><td>Instead of using physical counters, students can draw the counters and circle the groups on a whiteboard or in their books. Use this method to explain what is happening and as soon as they have understood what move on to the abstract method as this can be a time consuming process.</td><td>Image: Section of the section of th</td></t<>	Instead of using physical counters, students can draw the counters and circle the groups on a whiteboard or in their books. Use this method to explain what is happening and as soon as they have understood what move on to the abstract method as this can be a time consuming process.	Image: Section of the section of th

